# Mathematica 11.3 Integration Test Results

## Test results for the 97 problems in "8.10 Formal derivatives.m"

Problem 30: Result more than twice size of optimal antiderivative.

$$\int \! \frac{g[x] \ f'[x] + f[x] \ g'[x]}{1 - f[x]^2 \, g[x]^2} \, \mathrm{d}x$$

Optimal (type 9, 6 leaves, 2 steps):

ArcTanh[f[x] g[x]]

Result (type 9, 26 leaves):

$$-\frac{1}{2} Log[1-f[x]g[x]] + \frac{1}{2} Log[1+f[x]g[x]]$$

Problem 31: Result more than twice size of optimal antiderivative.

$$\int \! \frac{-g[x] \, f'[x] + f[x] \, g'[x]}{f[x]^2 - g[x]^2} \, \mathrm{d} x$$

Optimal (type 9, 8 leaves, 2 steps):

$$ArcTanh \left[ \frac{f[x]}{g[x]} \right]$$

Result (type 9, 23 leaves):

$$-\frac{1}{2} Log[f[x] - g[x]] + \frac{1}{2} Log[f[x] + g[x]]$$

Problem 32: Result more than twice size of optimal antiderivative.

$$\int \frac{f[x]^{-1+m} g[x]^{-1+n} \left( m g[x] f'[x] + n f[x] g'[x] \right)}{1 - f[x]^{2m} g[x]^{2n}} \, dx$$

Optimal (type 9, 10 leaves, 2 steps):

$$ArcTanh[f[x]^mg[x]^n]$$

Result (type 9, 34 leaves):

$$-\frac{1}{2} \, \text{Log} \Big[ 1 - f[x]^m \, g[x]^n \Big] + \frac{1}{2} \, \text{Log} \Big[ 1 + f[x]^m \, g[x]^n \Big]$$

#### Problem 33: Result more than twice size of optimal antiderivative.

$$\int \! \frac{f[x]^{\,\text{-1+m}}\,g[x]^{\,\text{-1+n}}\,\left(-\,\text{m}\,g[x]\,\,f'[x]\,\,+\,\text{n}\,f[x]\,\,g'[x]\right)}{f[x]^{\,\text{2m}}\,-\,g[x]^{\,\text{2n}}}\,\,\mathrm{d}x$$

Optimal (type 9, 12 leaves, 3 steps):

 $ArcTanh[f[x]^{-m}g[x]^n]$ 

Result (type 9, 31 leaves):

$$-\frac{1}{2} Log[f[x]^m - g[x]^n] + \frac{1}{2} Log[f[x]^m + g[x]^n]$$

#### Problem 34: Result more than twice size of optimal antiderivative.

$$\int \! \frac{f[x]^{\,\text{-1+m}}\,g[x]^{\,\text{-1-n}}\,\left(-\,\text{m}\,g[x]\,\,f'[x]\,-\,\text{n}\,f[x]\,\,g'[x]\right)}{f[x]^{\,\text{2\,m}}\,-\,g[x]^{\,\text{-2\,n}}}\,\text{d}x$$

Optimal (type 9, 14 leaves, 3 steps):

ArcTanh  $f[x]^{-m}g[x]^{-n}$ 

Result (type 9, 34 leaves):

$$-\frac{1}{2} Log \left[1-f[x]^{m} g[x]^{n}\right] + \frac{1}{2} Log \left[1+f[x]^{m} g[x]^{n}\right]$$

### Problem 43: Result more than twice size of optimal antiderivative.

Optimal (type 9, 8 leaves, ? steps):

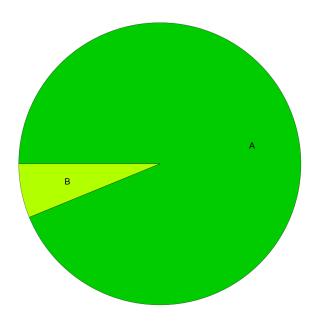
 $f[Sin[x]]g[e^x]$ 

Result (type 9, 28 leaves):

$$\left[\left(\mathsf{Cos}\left[\mathsf{x}\right]\mathsf{g}\left[\mathsf{e}^{\mathsf{x}}\right]\mathsf{f}'\left[\mathsf{Sin}\left[\mathsf{x}\right]\right]+\mathsf{e}^{\mathsf{x}}\mathsf{f}\left[\mathsf{Sin}\left[\mathsf{x}\right]\right]\mathsf{g}'\left[\mathsf{e}^{\mathsf{x}}\right]\right)\mathsf{d}\mathsf{x}\right]\right]$$

## **Summary of Integration Test Results**

#### 97 integration problems



- A 91 optimal antiderivatives
- B 6 more than twice size of optimal antiderivatives
- C 0 unnecessarily complex antiderivatives
- D 0 unable to integrate problems
- E 0 integration timeouts